Law, Science and Technology MSCA ITN EJD n. 814177





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Smart contracts and Proof of Location in Smart Cities

Outline

- Preliminaries
 - Authentication
- Introduction to Distributed Systems
 - Distributed systems
 - Blockchain
- Smart Contracts
 - Decentralized computing
- Proof of Location in Smart Cities
 - FOAM
 - Zero Knowledge PoL



Some preliminary notions

- Hash functions
- Digital signature
- Timestamp



f(x) = y

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Practically infeasible to invert:

 $f^{-1}(y) = ?$

f(x) = y

$$f(string) = digest$$



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SHA256

Cryptographic Hash function f(x) = yf(string) = digestSHA256(moat) = 98E2...16F3SHA256(maot) = E671...A9C9

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$$SHA256(mot) = E671...A9C9$$

digest length is always the same (256 bit in the case of SHA256)

Collision free : the probability of two inputs with the same digest is very small

SHA256

Digital Signature

Scheme for verifying the **authenticity** of digital messages (documents).

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Employs Asymmetric Cryptography:

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public key (associated to a pub certificate)private key

Integrity: grants that the message was not altered in transit (digest)



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public key (associated to a pub certificate)private key

Integrity: grants that the message was not altered in transit (digest) Authentication: A valid digital signature gives a recipient very strong reason to believe that the message was created by a known sender. When can you associate the pub key to an identity (e.g. the sender)?

+ eIDAS recognizes 3 e-signature types

Electronic signatures

eIDAS sets a foundation for all electronic signatures by asserting that no signature can be denied legal admissibility solely because it's in electronic form e.g.: Signing an e-mail with your personal name or entering a PIN code

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Electronic signatures

Advanced Electronic Signatures (AdES)

eIDAS sets a foundation for all electronic signatures by asserting that no signature can be denied legal admissibility solely because it's in electronic form e.g.: Signing an e-mail with your personal name or entering a PIN code

With AdES, signatures must be uniquely linked to, and capable of identifying, the signer. Signers create their signature using data solely under their control and the final document is tamper-evident.

← Digital Signatures

(XAdES, PAdES, CAdES, Associated Signature Container Baseline Profile without qualified Certificate, Graphometric signature, biometric signature, etc.)

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Electronic signatures

Advanced Electronic Signatures (AdES) Qualified Electronic Signatures (QES)

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← Digital Signatures

(XAdES, PAdES, CAdES, Associated Signature Container Baseline Profile without qualified Certificate, Graphometric signature, biometric signature, etc.)

QES is a stricter form of AdES. Same legal value as handwritten signatures. It requires signers to use certificate-based digital ID issued by a qualified EU Trust Service Provider (TSP), along with a qualified signature creation device (QSCD) e.g.: XAdES, PAdES, CAdES with Qualified Certificate and secure device: smart card, USB token, or mobile with a one-time passcode

Data in electronic form which binds other data in electronic form to a particular time establishing evidence that the latter data existed at that time

 links the date and time with the data so that the possibility of modifying the data without being detected is reasonably eliminated



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Legal validity of the qualified electronic time stamp

- Art. 41 of eIDAS
- A qualified electronic time stamp shall enjoy the presumption of the accuracy of the date and the time it indicates and the integrity of the data to which the date and time are bound.

+ In Italy

- The digital document signed with qualified digital signature(s) should be closed by a qualified time stamp in order to fix the date when the qualified certificate(s) of the digital signature(s) is/are valid.
- Over the time the qualified certificates expire and it is not possible to validate the validity of the certificates in the moment of the signature.

Digitally signed and time stamped Document





















Introduction to Distributed Systems

and Blockchains



Client/Server Architecture

A system architecture is the conceptual **model** that defines the **structure**, **behavior**, and more **views** of a system

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Client/Server Architecture Example

Alice pays Bob 5 euros





Server



Client/Server Architecture Example

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Peer to Peer (P2P) Architecture

Peers are Client and Server simultaneously



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Systems that don't share memory (or clock) but connect and relay information over a communication medium. The different nodes in distributed system have their own memory, OS and local resources.

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BLOCKCHAIN

╺╋╸

A Distributed System based on a P2P network





 It is a technology which is part of the realm of the DLT: Distributed Ledger Technologies

+ Blockchain

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- It is a technology which is part of the realm of the DLT: Distributed Ledger Technologies
- A ledger is distributed among nodes in a network, that update their local copy following a unique consensus mechanism
- A blockchain is a DLT where the ledger takes the form of a set of block (relatively) chronologically ordered

+ Blockchain we can distinguish between



How the ledger is structured: chain of blocks



Bi

Content of Bi:		
Transactions		
Others		



Bi





































+ Consensus: Proof of Work and propagation



+ Consensus: Proof of Work and propagation



+ Consensus: Proof of Work and propagation


+ Consensus: Proof of Work and propagation





Consensus: Fork





How the ledger is structured: chain of blocks

• What to write in the ledger: **transactions**





TX 1 TX 2 TX 3

+ Transactions

- If the ledger maintains the state of the system, a transaction is the operation that alters this state
- The state of the system at a certain time (snapshot) is a list of transactions

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TX 1 TX 2 TX 3 + TX 4

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 - The state of the system at a certain time (snapshot) is a list of transactions
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 - A valid transaction is signed using the digital signature of the account that holds the previous one

TX 1 TX 2 TX 3 + TX 4 TX 1 TX 2 TX 3 TX 4









Wallet







+ In Italy

- «the storage of a digital document using technology based on DLT produces legal effects of the time stamping of the article 41 of the regulation EU n. 919/2014....»
- «La memorizzazione di un documento informatico attraverso l'uso di tecnologie basate su registri distribuiti produce gli effetti giuridici della validazione temporale elettronica di cui all'articolo 41 del regolamento (UE) n. 910/2014 del Parlamento europeo e del Consiglio, del 23 luglio 2014.»



Alice pays Bob 5 euros



Alice pays Bob 5 bitcoin

It means to issue a new transaction in the blockchain, hence Alice must refer to a past TX were she received at least 5 bitcoin



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Smart Contracts

Ethereum



A Smart Contract is (simply) a program

that is executed by all the nodes in a blockchain network

```
* @param challengeID The challenge position in the list
* @param inFavour Boolean value indicating if in favour or not
function vote(uint256 challengeID, bool inFavour)
    public
    onlyEligible(challengeID)
    notExecuted(challengeID)
    Challenge storage chall = _challenges[challengeID];
    Vote storage v = chall.votes[msg.sender];
    require(!v.voted, "Voting: already voted");
    _vote(challengeID, inFavour);
    emit Voted(challengeID, msg.sender, inFavour);
```

Decentralized computing



Traditional apps make requests that are processed by one or a few servers

Decentralized computing



Traditional apps make requests that are processed by one or a few servers

dApps make requests that are processed by all the nodes in the blockchain network (Ethereum)

Decentralized Applications

Blockchain-based user-facing interfaces which connect the end user to the technology through a combination of underlying Smart Contracts



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Blockchain-based user-facing interfaces which connect the end user to the technology through a combination of underlying Smart Contracts





The relationship between dApps, Smart Contracts and the Blockchain is similar to traditional web applications. Client/server app interacts with a particular server to access its database.

Similarly, dApps use Smart Contracts in order to connect to the particular Blockchain upon which they are based (e.g. Ethereum).



1. If you have N independent nodes in a network and the majority $(\frac{2}{3} + 1)$ of them follows the same "consensus mechanism"

Trust without a third party

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- 2. If you trust the consensus mechanism (including also the source code it is built upon -> open source)

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then

you can trust the correct execution of the program





Collusion



The majority is honest

- When a Smart Contract has some bugs
 - -> assess the programming code before using it
 - -> use standards and common libraries (OpenZeppelin)

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 - -> assess the programming code before using it
 - -> use standards and common libraries (OpenZeppelin)
- When the blockchain code has some bugs
 - The DAO attack, 3.6 million ether robbed (~ 70\$ million)
 - Force the entire network to revert transactions in the ledger (difficult)



• Allow to easily maintain data structures in the blockchain

Ethereum Smart Contracts

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Ethereum Smart Contracts

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- A new transaction refers to a previous one and updates the state of the system
 - In this case the state of the system considers not only monetary transactions, but also data structures in smart contracts
 - The previous one refers to a transaction that holds the contract (machine) code
 - The new transaction indicate a piece of code to execute in the contract



Example: A voting operation in a Smart Contract







function vote(Challenge challenge, bool inFavour) public {
 if (inFavour) {
 challenge.inFavour.add(msg.sender); // Alice
 } else {
 challenge.against.add(msg.sender); // Alice
 }
}

Example: A voting operation in a Smart Contract

Proof Of Location

in Smart Cities









Crypto-Spatial Coordinate (CSC)

A standard for location in Ethereum Smart Contracts (SC)







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Spatial Index and Visualizer (SIV)

A **blockchain explorer** that enables users to engage and act with spatial data





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Proof of Location (POL)

Consensus on whether an event or agent is verifiably at a certain point in time and space

CSC allow any SC to make an immutable claim to a specific location, using:

• The location geohash



base32, 48 bits	base16, 160 bits	
dr5rehu19f	0x7d551397f74a2988b024afd0efe4ee802c7721bc	

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dr5rehu19f	0x7d551397f74a2988b024afd0efe4ee802c7721bc			
, 7		\		
base16, 256 bits				
0x3b0556fae1e22	8878fb35b24e0a5f9c4f13b59035ff899e03f56c0a192	50616		

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base58, 96 bits				
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A **registry SC** takes a CSC and decode its location and Ethereum address Any user can verify if a CSC is where it claims to be by visiting the location

The resolution is one square meter -> 500 trillion unique locations

A General Purpose Visual Blockchain Explorer front-end interface to visualize SC on a map.



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DEPLOY A SC

A SC is directly deployed using an Ethereum Wallet



A **General Purpose Visual Blockchain Explorer** front-end interface to visualize SC on a map.



referenced SC are displayed directly in the application



VISUALIZE NEW CSC New CSC-referenced SCs are automatically shown



DEPLOY A SC

A SC is directly deployed using an Ethereum Wallet x5b963b549a77a...

+ FOAM PROOF OF LOCATION

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Dynamic Pol

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Dynamic Pol

Provide consensus on whether an event or agent is verifiably at a certain point in time and space

- Used for Geographic Points of Interest (Pol)
- Token Curated Registries (TCRs) are a crypto-economic model for curating human readable lists of POI







1. Candidates submit a **FOAM Token deposit** in order to add a Pol to the registry They **wait out an initial challenge**







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 - b. If the challenging Cartographer succeeds, the Candidate's **deposit is distributed to the winning** Cartographers as a reward for helping to curate TCR







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 - b. If the challenge is unsuccessful, a percentage of the loser
 Cartographer's deposit is forfeited to the Candidate whose Pol was affirmed and to the winning Cartographers







Dynamic PoL (IoT guys!)

• FOAM PoL implementation is based on LPWAN, a new class of radio highly promising for IoT

Low Power Wide Area Networks



Dynamic PoL (IoT guys!)

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- LPWAN can offer the **low power** and **longer battery life** of bluetooth with the **range of cellular**, and access to the unlicensed radio spectrum



Low Power Wide Area Networks



Dynamic PoL (IoT guys!)

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- LPWAN can offer the **low power** and **longer battery life** of bluetooth with the **range of cellular**, and access to the unlicensed radio spectrum
- Trade-off are low data rate and higher latency
- One of the most promising new radios, LoRa, can travel 5–15km at 150 MHz and 1 GHz bands and provide bidirectional communication



Low Power Wide Area Networks



① 1. ANCHORS & AUTHORITIES

Independent Radio **beacons** (Anchors) and Radio **gateways** (Authorities) start participating in the network by deposing some FOAM Tokens





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紧 2. ZONE FORMATION

Authorities start to establish a Zone and pledge to offer **location services** that are enforced by a SC





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Anchors and Authorities send messages until a **consensus** can be formed on the precise time. This allows to calculate location and to determine the **network geometry**



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Zones can provide **Presence Claims** for Customers for a transaction fee.

Customer sends a broadcast message to the Zone and Authorities validate his presence through **Time Difference Of Arrival**
+ Dynamic PoL



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Zones reach consensus through a **local blockchain**. Verifiers incentivized to check this Zone blockchain for **frauds**

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6. PROOF OF LOCATION

Verifiers send Verified or Fraud Proofs to the Ethereum Blockchain and the PoL certificates are created

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Platin is a decentralized, incentivized and privacy preserving location credentials service



Secure Verification of Location Claims

User location detection is secured through the use of different mechanisms



Zero Knowledge Proof of Location

User data is protected using the Zero Knowledge Proof protocol

1. Sensor Fusion

Secure Verification of Location Claims

 Location-relevant sensors: GPS, Bluetooth, WiFi, cellular network and accelerometers

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2. Behavior Over Time

Secure Verification of Location Claims

 Location-relevant sensors: GPS, Bluetooth, WiFi, cellular network and accelerometers

- Tracks user behavior over longer periods of time and builds up users' reputation scores
- AI technologies enable to secure both sensor fusion and behavior over time (XAIN Technologies)

1. Sensor Fusion

2. Behavior Over Time

3. P2P Witnessing

Secure Verification of Location Claims

 Location-relevant sensors: GPS, Bluetooth, WiFi, cellular network and accelerometers

- Tracks user behavior over longer periods of time and builds up users' reputation scores
- Al technologies enable to secure both sensor fusion and behavior over time (XAIN Technologies)
- Users will be able to act as witnesses for each others' locations through the use of short-range communication
- Users' efforts in verifying other's location claims will be rewarded

Zero Knowledge Proof of Location

Protocol that allows a **Verifier** to test whether position committed by a **Prover** is inside or outside the radius of a service area, without revealing exact location



13 Zero Knowledge Proof of Location [1\2] Sphere Equation





 $(x-x_0)^2+(y-y_0)^2+(z-z_0)^2=R^2$

 $A(x,y,z)=O(x_0,\overline{y_0,z_0})$

Alice's position Reference point's position

13 Zero Knowledge Proof of Location [1\2] Sphere Equation





 $(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2 < d^2$

 $A(x,y,z)=O(x_0,\overline{y_0,z_0})$

Alice's position Reference point's position

13 Zero Knowledge Proof of Location [1\2] Sphere Equation





 $d^2 - (x - \overline{x_0})^2 - (y - y_0)^2 - (z - z_0)^2 > 0$

Alice's position

 $A(x,y,z) = O(x_0,y_0,z_0)$

Reference point's position

Zero Knowledge Proof of Location [2\2]





Lagrange Theorem

$$d^2 = (x-x_0)^2 = (y-y_0)^2 = (z-z_0)^2 = a_1^2 + a_2^2 + a_3^2 + a_4^2$$

No tuple exists for negative differences (points outside the range)

$$A(x,y,z) = O(x_0,y_0,z_0)$$

Alice's position

Reference point's position

Discrete logarithm to hide the secret



Let p and q be primes, n = pq. Then for some (properly chosen) positive g < n, the function: $f(u) = g^u \pmod{n}$

is a **one-way** function if p and q are unknown.

Hence Alice only needs to report values $g^x \pmod{n}$, $g^y \pmod{n}$ and $g^z \pmod{n}$ in order to let Bob verify the distance, without knowing A(x, y, z), through the equality:

$$g^{d^2-(x-x_0)^2-(y-y_0)^2-(z-z_0)^2}=g^{a_1^2+a_2^2+a_3^2+a_4^2}$$



Tokyo Olympics 2020



PLATIN Use case



I ask you:

Could Proof of Location be used as evidence?